

```

matC = 
$$\begin{pmatrix} 1 & -2 & 3 \\ 0 & 6 & 1 \\ 3 & 0 & 9 + 10i \end{pmatrix};$$

n = 3;
estimateEval[B_, α_, showMarkers_?BooleanQ, showLabel_?BooleanQ] :=
Module[{A, A1, A2, eval, circles, circleCentres, evalPoints},
Assert[α ≥ 0 && α ≤ 1, "α must be in the range [0;1]"];
A1 = DiagonalMatrix[Diagonal[B]];
A2 = B - DiagonalMatrix[Diagonal[B]];
A = A1 + α * A2;

eval = Eigenvalues[A] // N;
circles = Table[
Circle[{Re[A[[i, i]]], Im[A[[i, i]]]}, Total[Abs[A[[i, Cases[Range[1, n], x_ /; x ≠ i]]]]]],
{i, 1, n}];
circleCentres = Table[
Callout[
{Re[A[[i, i]]], Im[A[[i, i]]]},
Subscript["d", ToString[i] <> ToString[i]]
],
{i, 1, n}];
evalPoints = Table[
Callout[
{Re[eval[[i]]], Im[eval[[i]]]},
Subscript["λ", i],
{Re[eval[[i]]] - 0.8, Im[eval[[i]]] + 0.8}
],
{i, 1, n}] // N;

Show[
ListPlot[ { circleCentres showMarkers,
ListPlot[ [(#1[[1]]) &/@circleCentres True ,
PlotRange → {{-5, 14}, {-6, 14}},
PlotStyle → □,
PlotMarkers → {"♦", 14},
AxesLabel → {"Re", "Im"},
ImageSize → Large,
BaseStyle → {FontSize → 14},
AspectRatio → Automatic,
PlotLabel → [{"α = " <> ToString[Round[α, 0.01]] showLabel
True
}],
ListPlot[ { evalPoints showMarkers , PlotStyle → □, PlotMarkers → {"●", 12}],
Legended[
Graphics[
{
□, Thickness[0.004], circles,
Opacity[0.1], Disk @@ circles
}
]
,
PointLegend[{□, □}, {"Circle centre", "Eigenvalue"}, LegendMarkerSize → 14, LegendMarkers → {"♦", 14}, {"●", 11}]]}
]
]
]

```

```
Manipulate[
 estimateEval[matC,  $\alpha$ , showMarkers, True]
 , { $\alpha$ , 0, 1}, {showMarkers, {True, False}}]
```

$\alpha$

showMarkers

```
estimateEval[matC, 1., True, True]
```

```
(*Export[FileNameJoin[{NotebookDirectory[], "frames/showMarker=0alpha=00.png"}],
Table[estimateEval[matC, $\alpha$ ,False,True],{ $\alpha$ ,0,1,0.05}],"VideoFrames",Antialiasing→True];
Export[FileNameJoin[{NotebookDirectory[], "frames/showMarker=1alpha=00.png"}],
Table[estimateEval[matC, $\alpha$ ,True,True],{ $\alpha$ ,0,1,0.05}],"VideoFrames",Antialiasing→True];*)
```

$$\text{Eigenvalues}\left[\begin{pmatrix} f_{11} & 0 \\ 0 & f_{22} \end{pmatrix} + \alpha \begin{pmatrix} 0 & f_{12} \\ f_{21} & 0 \end{pmatrix}\right]$$

$$\left\{\frac{1}{2} \left(f_{11}+f_{22}-\sqrt{f_{11}^2+4 \alpha^2 f_{12} f_{21}-2 f_{11} f_{22}+f_{22}^2}\right), \frac{1}{2} \left(f_{11}+f_{22}+\sqrt{f_{11}^2+4 \alpha^2 f_{12} f_{21}-2 f_{11} f_{22}+f_{22}^2}\right)\right\}$$

```
estimateEval[matC, 1, True, False]
```

